

# STRUCTURE TENSOR BASED SYNTHESIS OF DIRECTIONAL TEXTURES FOR VIRTUAL MATERIAL DESIGN

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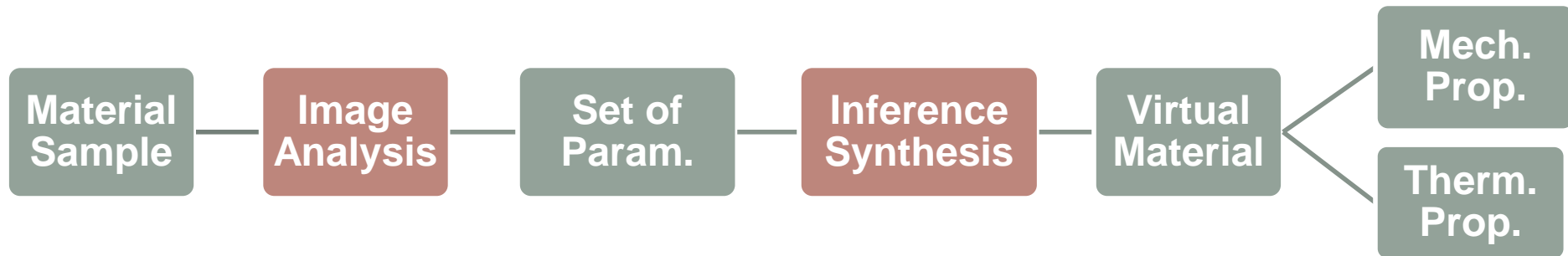
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# Virtual Material Design

## Motivation:

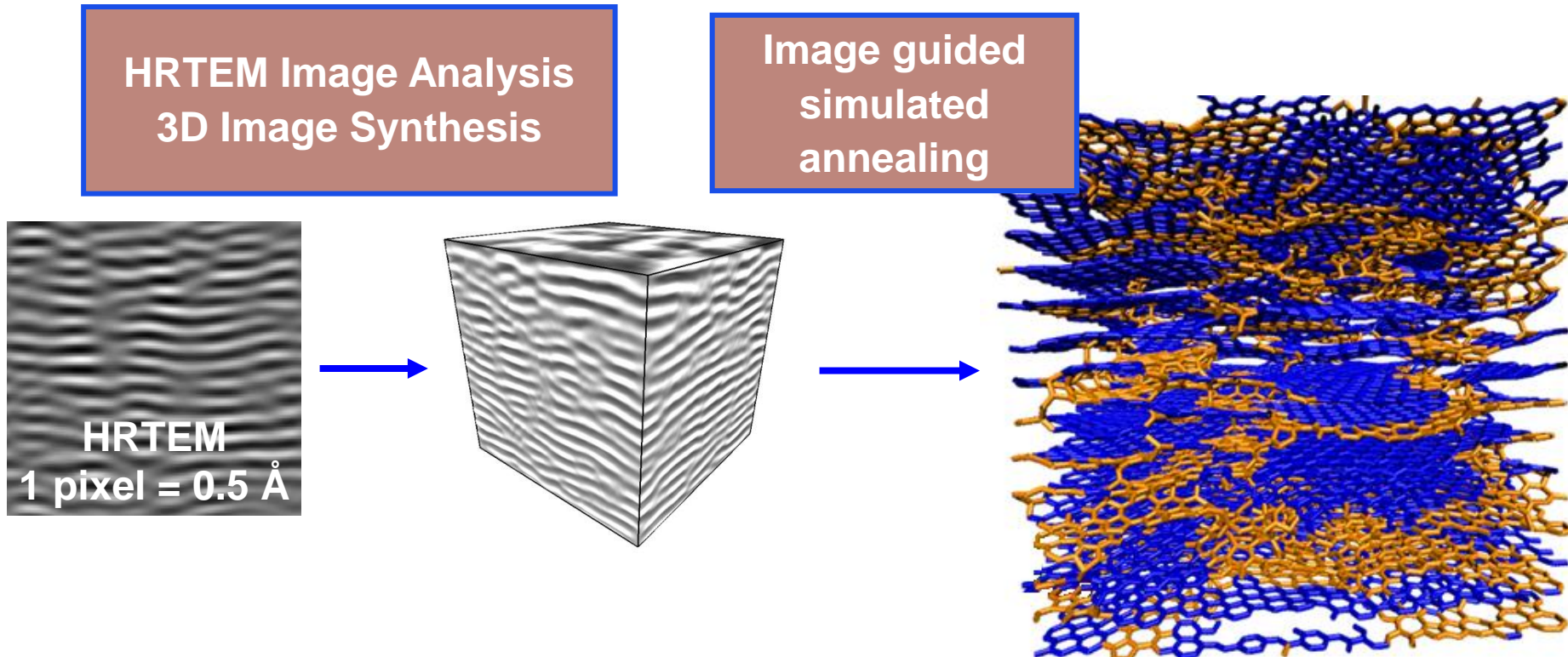
To produce “in silico material” from parameters extracted from image analysis of real material samples.



# Virtual Material Design

Pyrocarbon at atomic scale :

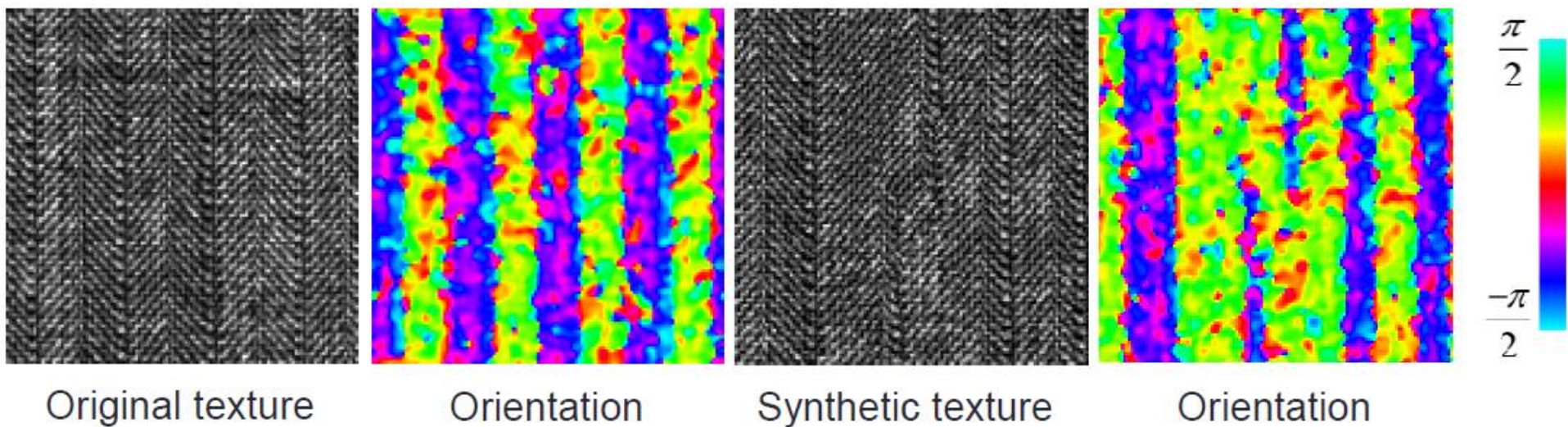
- Image Guided Atomistic Reconstruction
- High Resolution Transmission Electronic Microscope (HRTEM)



# Previous works

## Structured anisotropic textures synthesis:

- Non parametric approaches [2] tend to produce more regular textures than the exemplar
- Parametric approaches [3] produce unexpected artifacts
- Both fail on highly structured and non homogeneous textures



[2] L.-Y. Wei and M. Levoy, "Fast texture synthesis using tree-structured vector quantization," Proc. of ACM SIGGRAPH 2000.

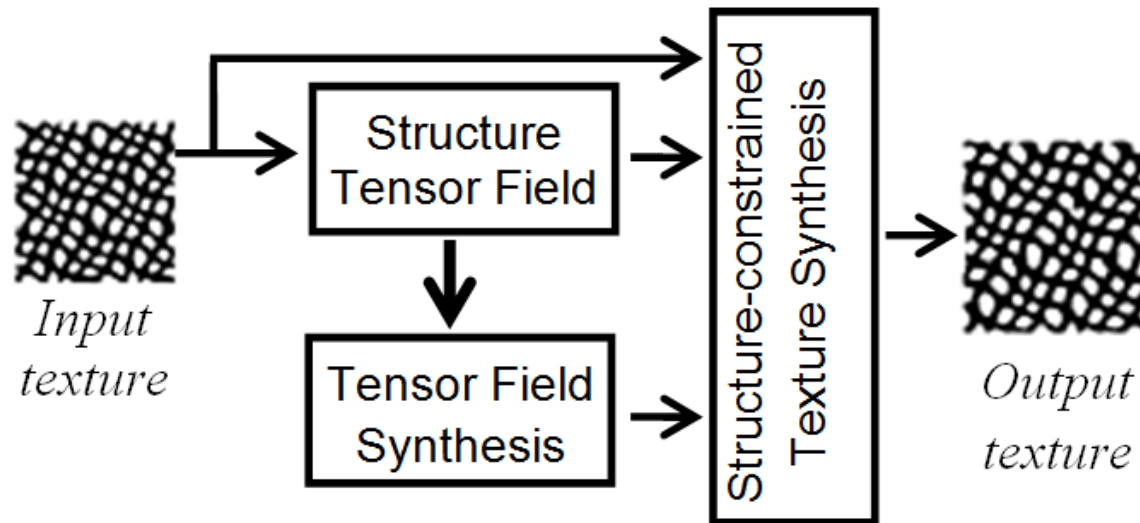
[3] J. Portilla and E. P. Simoncelli, "A Parametric Texture Model based on Joint Statistics of Complex Wavelet Coefficients". Int'l Journal of Computer Vision. 2000

# Proposed approach

As in [4], we take into account a “geometric layer”

Our approach combines :

- A prior synthesis of a geometric layer (structure tensor)
- A non parametric synthesis algorithm guided by the geometric layer (derived from [2])



[2] L.-Y. Wei and M. Levoy, "Fast texture synthesis using tree-structured vector quantization," Proc. of ACM SIGGRAPH 2000.

[4] G. Peyré, "Texture Synthesis with grouplets". IEEE Trans. on Pattern Analysis and Machine Intelligence, 32(4):733-746, 2009.



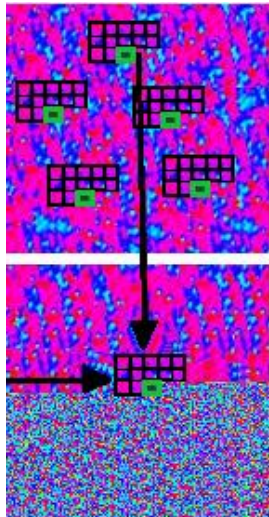
# Texture tensor field synthesis

Based on Wei and Levoy algorithm [2]

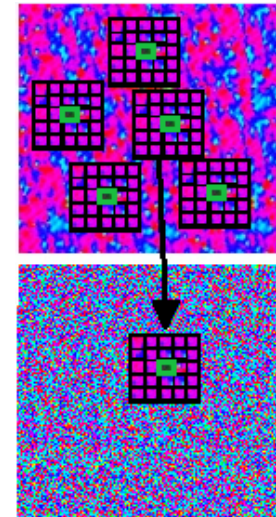
Adapted to the specificities of tensor-valued images

=> Synthesis of a tensor field similar to the exemplar's:

Causal neighborhood with a  
lexicographical scan



Square non-causal neighborhood with  
a random walk



# Texture tensor field synthesis

Structure tensor field  $S = G_\sigma * (\nabla I \cdot \nabla I^t)$

$$S(x, y) = \begin{bmatrix} S_{xx}(x, y) & S_{xy}(x, y) \\ S_{xy}(x, y) & S_{yy}(x, y) \end{bmatrix}$$

Coherence  $C(S)$  is computed from the eigenvalues  $\lambda_i$

$$C(S) = (\lambda_1(S) - \lambda_2(S)) / (\lambda_1(S) + \lambda_2(S))$$

Orientation  $O(S)$  is obtained from the 1<sup>st</sup> eigenvector  $[e_x, e_y]$ :

$$O(S) = \tan^{-1}(e_y / e_x)$$

# Texture tensor field synthesis

Tensor neighborhoods are compared:  
using the sum of their tensor dissimilarities

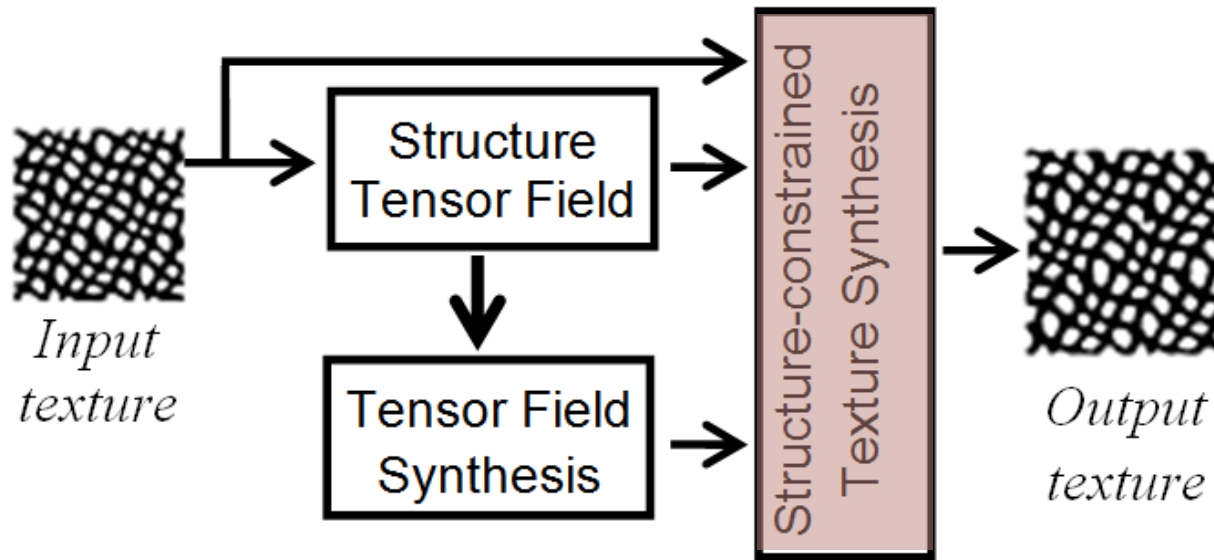
$$STD(F_1, F_2) = \sum_{n=1}^N M_i(F_1(n), F_2(n)); \quad i \in \{1, 2, 3, 4\},$$

Four tensor-space metrics  $M_i$  are considered:

- Euclidean distance  $M_1$
- Shape-Orientation metric:  $M_2$
- Frobenius norm  $M_3$
- Log-Euclidean metric  $M_4$



# The structure/texture approach



Combining Tensor domain and Pixel domain

$$D = p \cdot SSD(G_{in}, G_{out}) + (1 - p) \cdot STD(F_{in}, F_{out})$$

Pixel domain: SSD (Sum Square Distance)

Tensor domain: STD (Sum of Tensor Dissimilarity)

$p$ : weight assigned to each domain

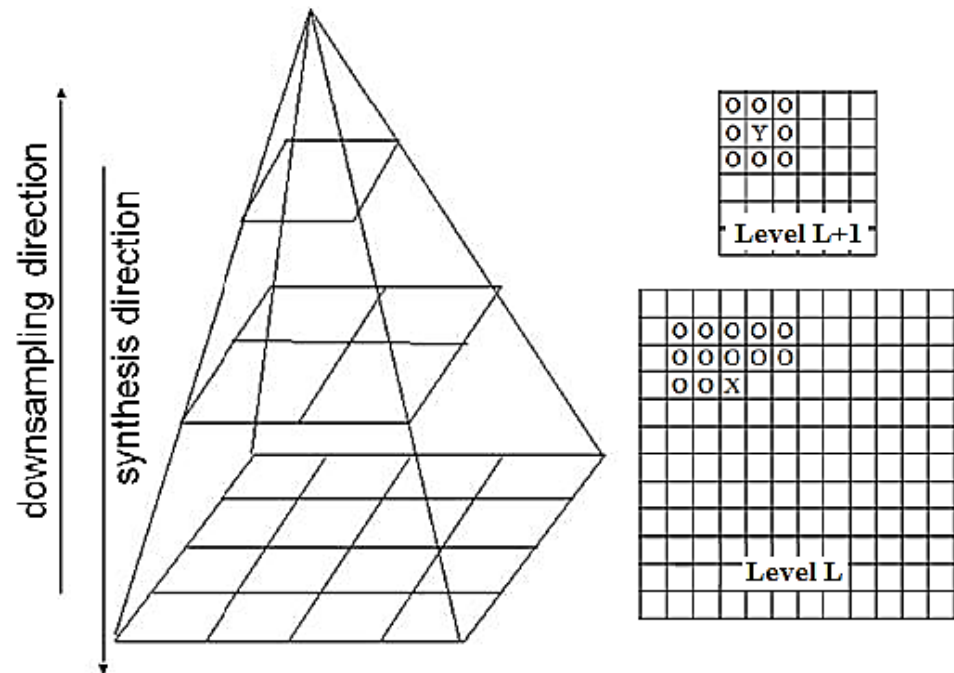
# Texture tensor field synthesis

Multi-resolution pyramids : avoid the use of large neighborhoods

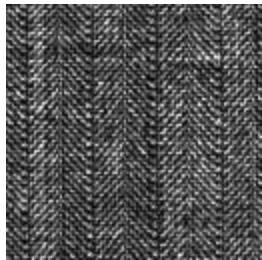
- Smoothing the tensor field with a Gaussian kernel
- Down-sampling with a 2:1 factor for each additional scale

Multi-resolution neighborhood of the tensor at level  $L$ :

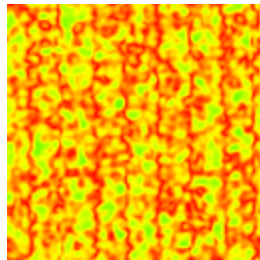
{ Level L neighborhood  
+  
Neighborhood of the  
tensor at level L+1



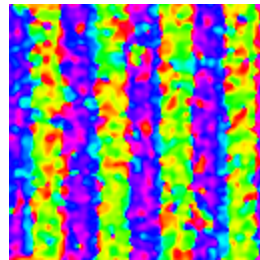
# Results



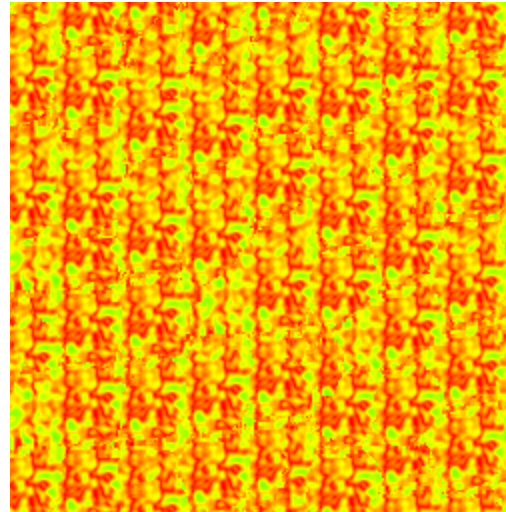
*Input  
texture*



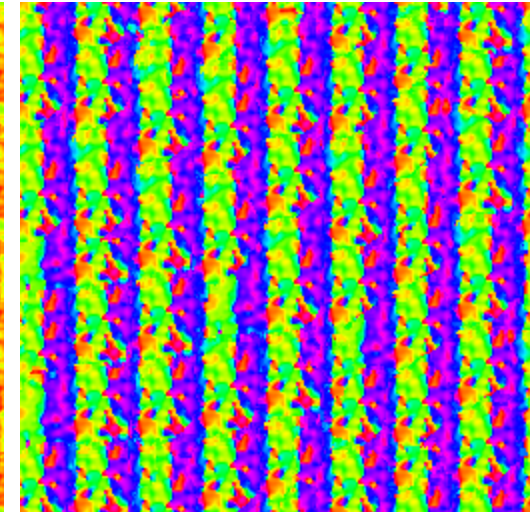
*Coherence*



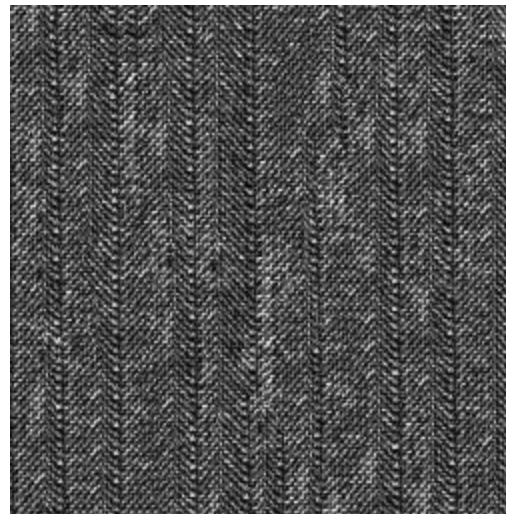
*Orientation*



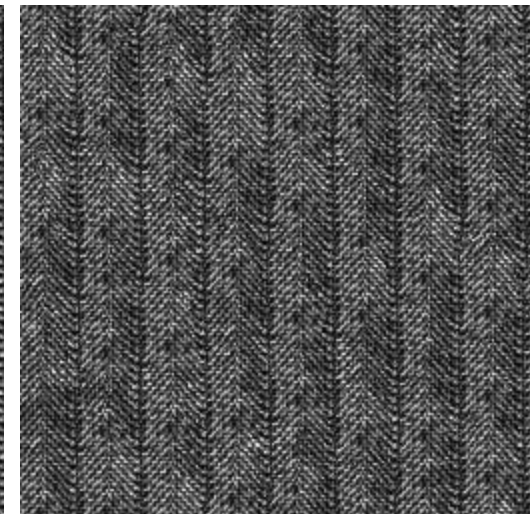
*Synthetic coherence image*



*Synthetic orientation image*

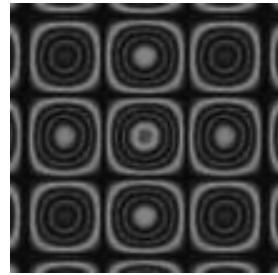


*Synthetic texture by W&L*

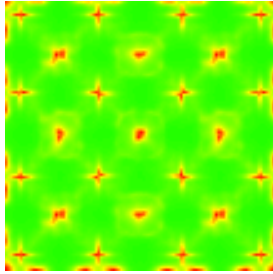


*Synthetic texture by the  
proposed approach*

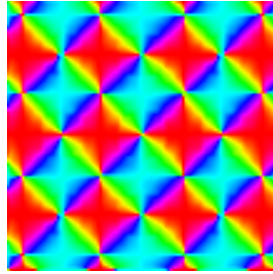
# Results



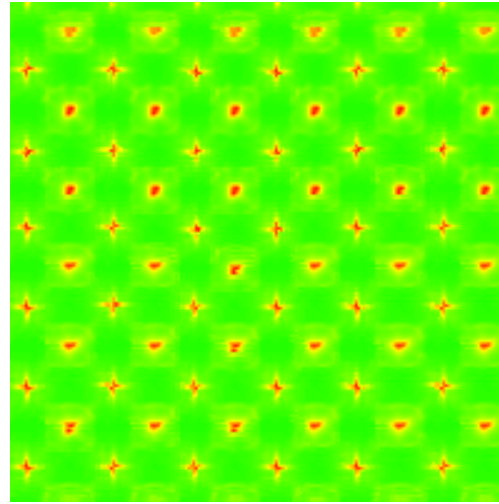
*Input  
texture*



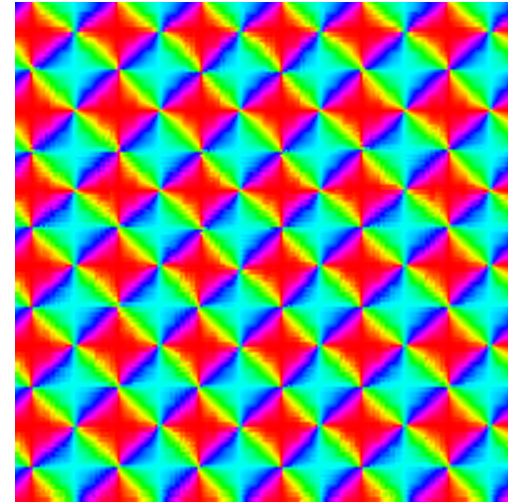
*Coherence*



*Orientation*



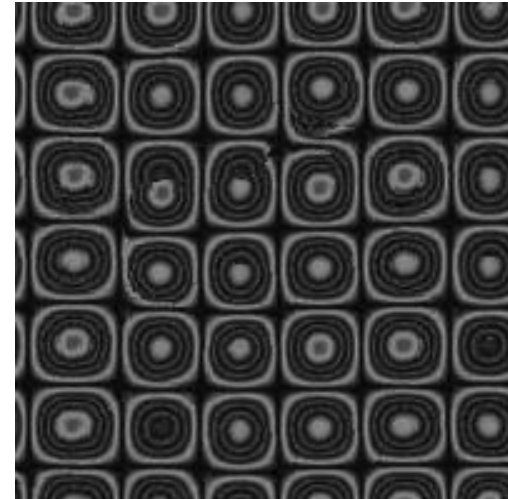
*Synthetic coherence image*



*Synthetic orientation image*



*Synthetic texture by W&L*

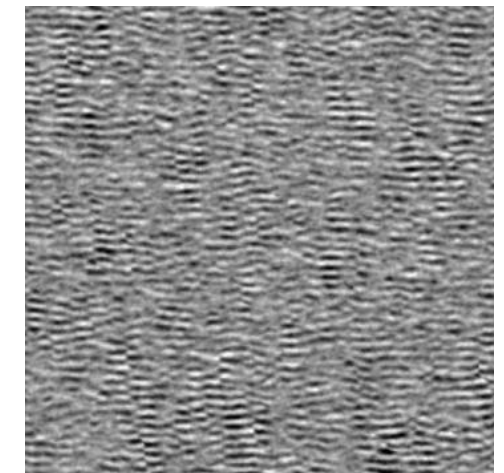
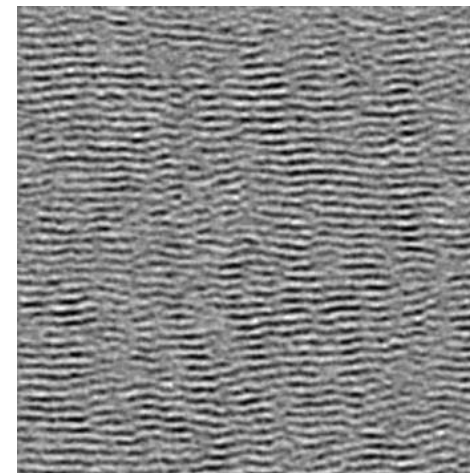
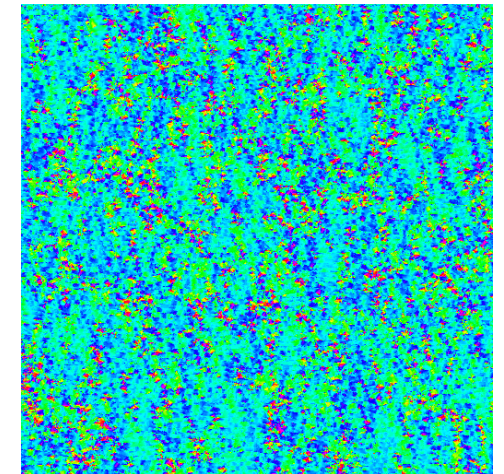
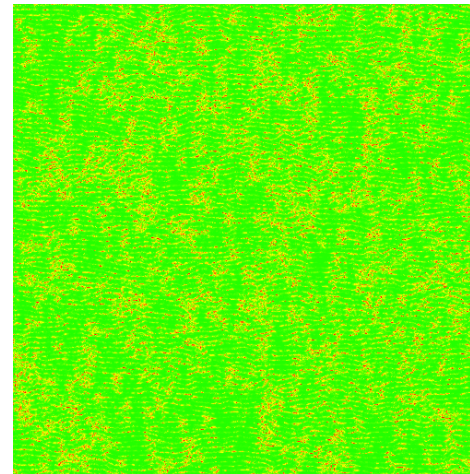
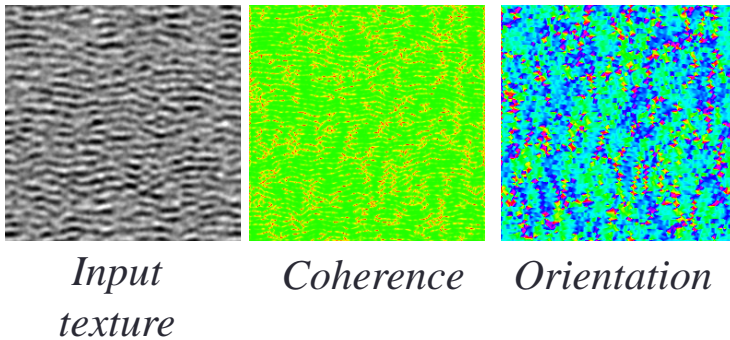


*Synthetic texture by the  
proposed approach*



# Results for virtual material

Preliminary results on pyrocarbon HRTEM images (2D)



# Conclusions & Prospects

## Non-parametric methods

- Tend to produce textures more regular than wanted

## The proposed approach

- multi-stage structure/texture synthesis
- Accurately reproduces the exemplar's variations of orientation

## Prospects

- Objective measures for evaluation
- Synthesis of non-stationary textures
- 3D extension
- Synthesis of material samples showing laminar structures



Thank you! Any questions ?

